

Controlling Bias & Confounding

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August 5th, 2015



QUESTIONS FOR BIAS

Key concepts

■ Bias

→ Should be minimized at the designing stage.

■ Random

→ Is the nature of the error. **We can do nothing at the analysis stage!**

■ Non-differential

→ Is the nature of (inaccurate) measurement.

■ Confounding

→ Indicative of true association. Can be controlled at the designing or **analysis** stage.

Is the following study acceptable?

- **We want to compare the mean of blood pressure levels between two groups.**
- **The blood pressure checker has a problem and always gives 5mmHg-higher than true values.**
- **All subjects were examined by the same blood pressure checker.**



Proper comparison between groups :

1) Comparison using accurate data

2) Comparison using (in)accurate data

As long as the magnitude of random error and bias of the two groups.

What would be the problem in this study?



**FOR DISCRETE VARIABLES,
MEASUREMENTS ERROR IS
CALLED **CLASSIFICATION ERROR**
OR **MISCLASSIFICATION****

Two types of misclassification

■ **Non-differential** misclassification

- Misclassification of a study variable that is independent of other study variables
- Systematic error may not be a critical issue as long as it occurs in all comparison groups.

■ **Differential** misclassification

- If the error occurs in one group due to bias away from null.

This is a problem!!

Non-differential Misclassification with Two Exposure Categories

Correct Data

	Exposed	Unexposed
Cases	240	200
Controls	240	600

$$OR = 3.0$$

Sensitivity = 0.8

Specificity = 1.0

	Exposed	Unexposed
Cases	192	248
Controls	192	648

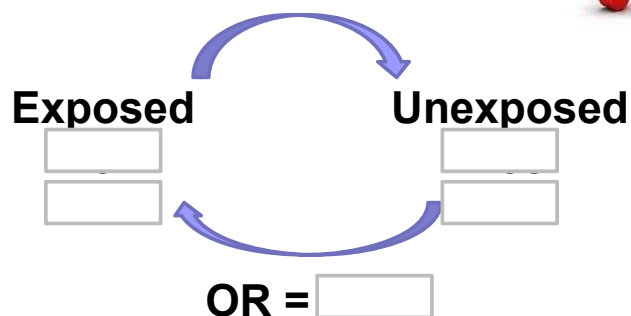
20% of exposed subjects were misclassified

$$OR = 2.61$$

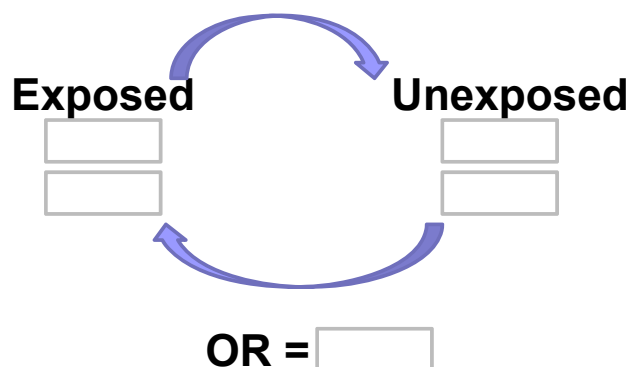
**What is the number of each cell?
Please calculate OR.**



Sensitivity = **0.8**
Specificity = **0.8**
Cases
Controls

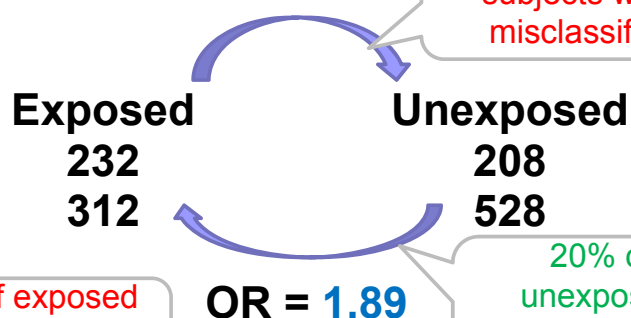


Sensitivity = **0.4**
Specificity = **0.6**
Cases
Controls

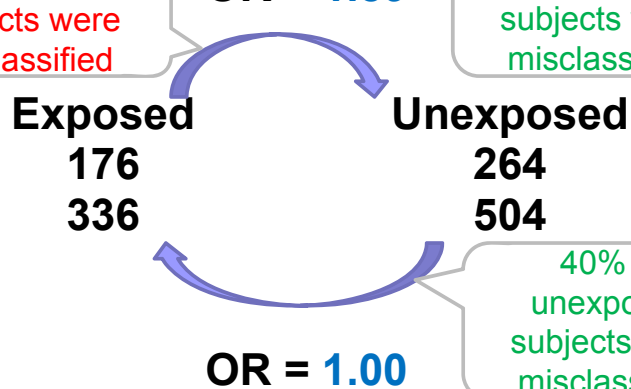


Non-differential Misclassification with Two Exposure Categories

Sensitivity = **0.8**
Specificity = **0.8**
Cases
Controls



Sensitivity = **0.4**
Specificity = **0.6**
Cases
Controls





How do you solve the problem of non-differential misclassification?



BIAS IN EPIDEMIOLOGIC STUDY

Different types of bias

- **Selection bias:**
It occurs at sampling

- **Detection bias:**
It occurs at diagnosis (outcome)

- **Measurement (information) bias:**
It occurs at surveillance

- ☐ **Recall bias**

- ☐ **Family information bias**

You need to plan your study design carefully.



You suspect that exposure to electromagnetic field (EMF) increases the risk of childhood leukemia. And, you conducted a case-control study.



- If parents of **cases** with leukemia, **living in the neighborhood of power lines**, suspect the association and **tend to agree on participation** to the study,

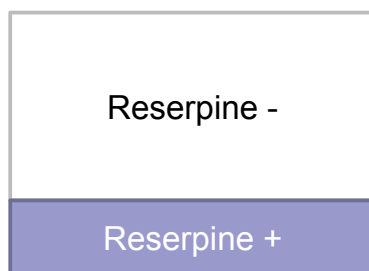


the association may become than what it should be.

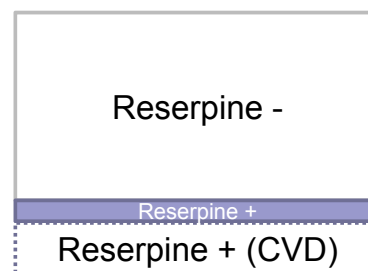
What is this bias? How do you solve it?

In a hospital-based case-control study, the researchers excluded subjects with CVD, whom "Reserpine" was likely to be prescribed, from control group.

They found that "Reserpine was a significant risk factor of breast cancer".



Cases: Breast cancer patients



Controls: Patients at the same hospital

Do you agree with their conclusion?

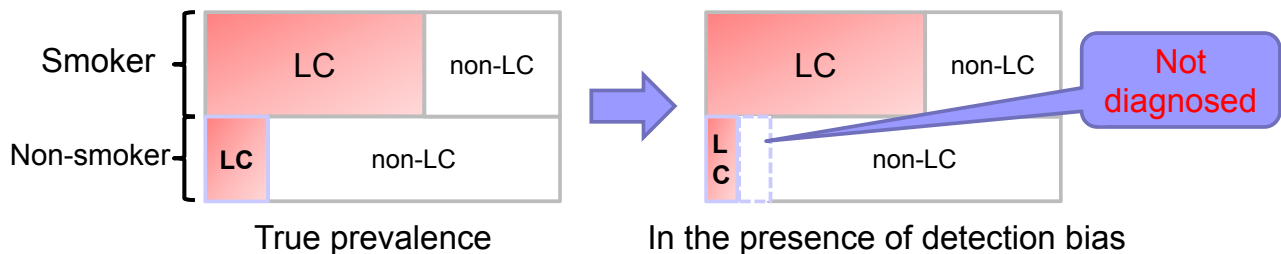


- **If you agree, why do you think so?**
- **If you don't agree, why do you think so? How do you solve it?**

A doctor may examine the patient's chest X-ray more carefully if he knew the patient is a heavy smoker but not for non-smoking patients.



→ **the association may become than what it should be.**



What is this bias?

Detection bias

How do you avoid detection bias?



Suppose, you conducted a case-control study on relationship of prenatal infections and congenital malformations.

You asked mothers regarding prenatal episode of infections by interview / questionnaire.

Cases
(mothers of babies with defect)



Controls
(mothers of healthy babies)



What is the possible bias?

Recall bias

How do you avoid / minimize the bias?

Consider using a hospital control



Controlling for misclassification

- - **Blinding**
 - prevents investigators and interviewers from knowing case/control or exposed/non-exposed status of a given participant
- - **Form of survey**
 - mail may impose less “white coat tension” than a phone or face-to-face interview
- - **Questionnaire**
 - use multiple questions that ask same information
- - **Accuracy**
 - Multiple checks in medical records & gathering diagnosis data from multiple sources

Lecture note of Dr. Dorak (<http://www.dorak.info/epi>)



CONFOUNDING

3 conditions of Confounding

- 1. Confounders are **risk factors** for the outcome.**
- 2. Confounders are **related to exposure** of your interest.**
- 3. Confounders are **NOT on the causal pathway** between the exposure and the outcome of your interest.**

How can we solve the problem of confounding?

“Prevention” at study design

- ✓ **Limitation**
- ✓ **Randomization** in an intervention study
- ✓ **Matching** in a cohort study

Notice: Matching does not always prevent the confounding effect in a case-control study.



How can we solve the problem of confounding?

“Treatment” at statistical analysis

- ✓ **Stratification** by a confounder
- ✓ **Multivariable / multiple analysis**



Mantel–Haenszel odds ratio

- **Stratification by confounding factor**
 - After stratification by confounding factor, **common OR, OR_{MH}** , among all strata should be calculated.
 - Assumption: there is a common OR among all strata → there is no significant difference in ORs among all strata by homogeneity test.

An example of Mantel-Haenszel estimation 1

Calculate the common OR among all strata

smoking	Case	Control	
+	a_i	b_i	M_{1i}
-	c_i	d_i	M_{0i}
Total	N_{1i}	N_{0i}	T_i

$$OR_c = \sum W_i OR_i / \sum w_i$$

i : "i" th stratum, W_i : weight of "i" th stratum

Practice 1

Mantel-Haenszel odds ratio(1)

1. Open the "tsunagi_v1" data by excel
☐ Please refer Appendix1 for the explanation of each variable.
2. Import this data set by your statistical software (STATA, R, and SPSS ...)

Mantel-Haenszel odds ratio(2)

3. Suppose, you want to examine the cancer risk by habitual alcohol drinking.

- Please **create a contingency table** of cancer and alcohol drinking.

STATA command: **tab alc cancer, row**

- Please **calculate an odds ratio**.

STATA command: **cc cancer alc**
or **cs cancer alc, or**

Same OR but 95%CI is slightly different

Case-control study

```
. cc cancer alc
```

	Exposed	unexposed	Total	Proportion Exposed
Cases	79	77	156	0.5064
Controls	316	738	1054	0.2998
Total	395	815	1210	0.3264
	Point estimate		[95% Conf. Interval]	
Odds ratio	2.396104		1.678901	3.416628 (exact)
Attr. frac. ex.	.5826558		.4043721	.7073138 (exact)
Attr. frac. pop	.2950629			

chi2(1) = 26.38 Pr>chi2 = 0.0000

Cohort study

```
. cs cancer alc, or
```

	alc			
	Exposed	Unexposed	Total	
Cases	79	77	156	
Noncases	316	738	1054	
Total	395	815	1210	
Risk	.2	.0944785	.1289256	
	Point estimate		[95% Conf. Interval]	
Risk difference	.1055215		.0612577	.1497852
Risk ratio	2.116883		1.584051	2.828946
Attr. frac. ex.	.5276074		.3687071	.6465115
Attr. frac. pop	.2671858			
Odds ratio	2.396104		1.706524	3.364381 (Cornfield)

chi2(1) = 26.38 Pr>chi2 = 0.0000

Mantel-Haenszel odds ratio(3)

4. Since we know that cancer risk increases with age, you may want to confirm the association between alcohol drinking and cancer risk by age group (<60 , $60-69$, ≥ 70).

☐ Please **create contingency tables** of cancer

STATA : **by age_gp, sort: tab alc cancer, row**

☐ Please **calculate odds ratios for each age group**.

An example of Mantel-Haenszel estimation 1

	age	alcohol	Case Control		OR
1	<60	+	13	129	1.54
		-	14	214	1 (ref)
2	60-69	+	32	105	3.95
		-	19	246	1 (ref)
3	≥70	+	34	82	2.62
		-	44	278	1 (ref)
Total		+	79	316	2.40
		-	77	738	1

Mantel–Haenszel odds ratio(5)

You can also calculate OR_{MH} by yourself.

$$OR_{MH} = \Sigma(a_i * d_i / T_i) / \Sigma(b_i * c_i / T_i)$$

$$OR_{MH} = \frac{(13*214/370) + (32*246/402) + (34*278/438)}{(129*14/370) + (105*19/402) + (82*44/438)}$$
$$= 2.69$$

Practice 2

1. Using the “*tsunagi_v1*” data set, please examine the association between habitual alcohol drinking and cancer risk by sex stratification.



```
. cc cancer alc, by(male)
```

male	OR	[95% Conf. Interval]		M-H weight	
0	.9455128	.3977241	2.01076	7.399209	(exact)
1	1.992308	1.179265	3.441301	11.52993	(exact)
Crude	2.396104	1.678901	3.416628		(exact)
M-H combined	1.583126	1.061639	2.360773		

Test of homogeneity (M-H) $\chi^2(1) = 2.68$ $Pr>\chi^2 = 0.1014$

Test that combined OR = 1:
Mantel-Haenszel $\chi^2(1) = 4.86$
 $Pr>\chi^2 = 0.0276$

Q1. Is this OR_{MH} statistically significant?

Q2. Is it OK to report OR_{MH} when the homogeneity test is statistically significant?



How can we solve the problem of confounding?

“Treatment” at statistical analysis

- ✓ Stratification by a confounder
- ✓ **Multivariable / multiple** analysis

Multivariate $\neq$ Multivariable (Multiple)

Am J Public Health. 2013 January; 103(1): 39–40.
Published online 2013 January. doi: [10.2105/AJPH.2012.300897](https://doi.org/10.2105/AJPH.2012.300897)

PMCID: PMC3518362
NIHMSID: NIHMS514677

Multivariate or Multivariable Regression?

Bertha Hidalgo, PhD, MPH[✉] and Melody Goodman, PhD, MS

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See letter "[Hidalgo and Goodman Respond](#)" in volume 10 on page e1.

This article has been [cited by](#) other articles in PMC.

Abstract

Go to: ☒

The terms multivariate and multivariable are often used interchangeably in the public health literature. However, these terms actually represent 2 very distinct types of analyses. We define the 2 types of analysis and assess the prevalence of use of the statistical term multivariate in a 1-year span of articles published in the American Journal of Public Health. Our goal is to make a clear distinction and to identify the nuances that make these types of analyses so distinct from one another.

Multivariable (Multiple) analysis

A multivariable model can be thought of as a model in which multiple variables are found on the right side of the model equation. This type of statistical model can be used to attempt to assess the relationship between a number of variables; one can assess independent relationships while adjusting for potential confounders.

This is the model to control the effects of confounders!

By contrast, a multivariable or multiple linear regression model would take the form

$$(2) y = \alpha + x_1\beta_1 + x_2\beta_2 + \dots + x_k\beta_k + \varepsilon$$

where y is a continuous dependent variable, x is a single predictor in the simple regression model, and $x_1, x_2, \dots, x_k$ are the predictors in the multivariable model.

As is the case with linear models, logistic and proportional hazards regression models can be simple or multivariable. Each of these model structures has a single outcome variable and 1 or more independent or predictor variables.



Multivariate analysis

Multivariate, by contrast, refers to the modeling of data that are often derived from longitudinal studies, wherein an outcome is measured for the same individual at multiple time points (repeated measures), or the modeling of nested/clustered data, wherein there are multiple individuals in each cluster. A multivariate linear regression model would have the form

$$(3) Y_{n \times p} = X_{n \times (k+1)} \beta_{(k+1) \times p} + \epsilon$$

where the relationships between multiple dependent variables (i.e., Y_s)—measures of multiple outcomes—and a single set of predictor variables (i.e., X_s) are assessed.

This model is to analyze the relationship between “multiple outcomes” and a single set of predictors.



LOGISTIC REGRESSION ANALYSIS

Practice 3

Multivariable analysis

1. Let's see the association between habitual alcohol drinking and cancer risk by logistic regression model.

STATA : **logistic cancer alc**
or **logit cancer alc, or**

2. Please examine this association adjusting for the effects of age and sex.



STATA : **logistic cancer alc male age**

. logistic cancer alc male age						
Logistic regression						
Log likelihood = -431.32695			Number of obs	=	1210	
			LR chi2(3)	=	67.45	
			Prob > chi2	=	0.0000	
			Pseudo R2	=	0.0725	
cancer	Odds Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
alc	1.877452	.3864541	3.06	0.002	1.254174	2.810476
male	2.099375	.4306218	3.62	0.000	1.404405	3.138251
age	1.041058	.0093757	4.47	0.000	1.022844	1.059597

STATA : **logistic cancer alc male age_gp**

```
. logistic cancer alc male age_gp
```

```
Logistic regression               Number of obs   =      1210
                                LR chi2(3)          =       66.37
                                Prob > chi2         =      0.0000
Log likelihood = -431.86621        Pseudo R2       =      0.0714
```

cancer	Odds Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
alc	1.825007	.3736455	2.94	0.003	1.221779	2.726067
male	2.198312	.4481714	3.86	0.000	1.474193	3.278117
age_gp	1.669985	.1951521	4.39	0.000	1.328136	2.099824

STATA : **xi: logistic cancer alc male i.age_gp**

Categorical variable (>2 categories)

```
. xi: logistic cancer alc male i.age_gp
```

```
i.age_gp      _Iage_gp_1-3      (naturally coded; _Iage_gp_1 omitted)
```

```
Logistic regression               Number of obs   =      1210
                                LR chi2(4)          =       66.47
                                Prob > chi2         =      0.0000
Log likelihood = -431.81689        Pseudo R2       =      0.0715
```

cancer	Odds Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
alc	1.825179	.3735059	2.94	0.003	1.222123	2.725812
male	2.192979	.4473008	3.85	0.000	1.470332	3.270798
_Iage_gp_2	1.792761	.4573496	2.29	0.022	1.087359	2.955776
_Iage_gp_3	2.84385	.6937492	4.28	0.000	1.763025	4.587276

If there is no linear trend of the cancer risk by age, it would be better to use categorical variable for age.



REGRESSION ANALYSIS

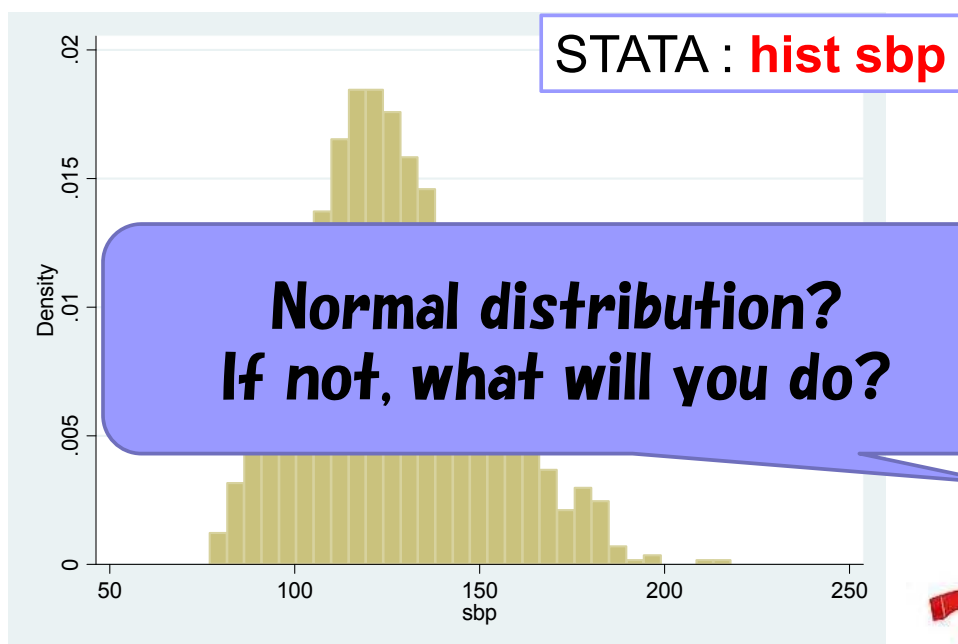


Practice 4 Regression analysis (1)

- Suppose, you want to know predictors of **systolic blood pressure** in the subjects of “tsunagi_v1” data.
- What do you have to check first?

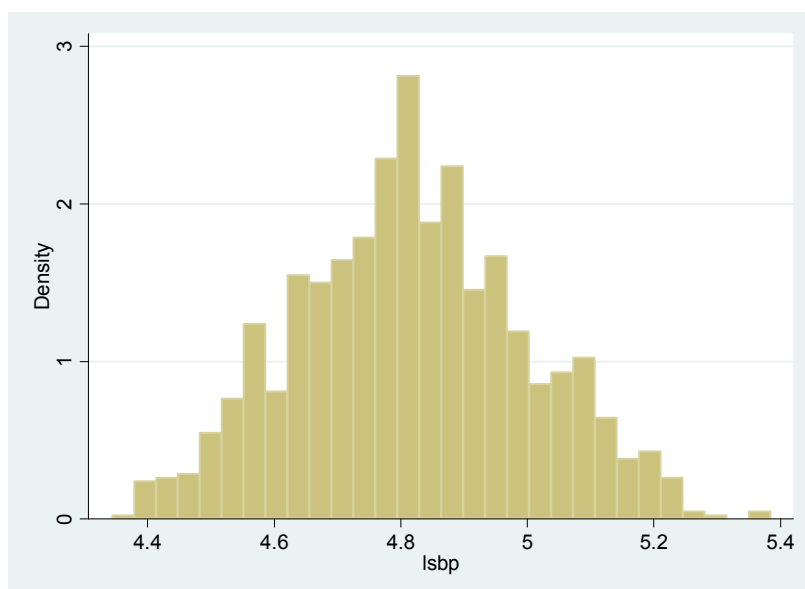


Distribution of systolic blood pressure



Log-transformation may work...

STATA : **gene lsbp=log(sbp)**
hist lsbp



Practice 4

Regression analysis (2)

- Age is one of the predictors of systolic blood pressure.
- Please conduct regression analysis using "age" as a explanatory variable.

STATA : **reg lsbp age**



STATA commands

. reg lsbp age						
Source	SS	df	MS			
Model	2.84842138	1	2.84842138	Number of obs = 1210		
Residual	37.4400935	1208	.030993455	F(1, 1208) = 91.90		
Total	40.2885149	1209	.033323834	Prob > F = 0.0000		
				R-squared = 0.0707		
				Adj R-squared = 0.0699		
				Root MSE = .17605		
lsbp	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
age	.0044274	.0004618	9.59	0.000	.0035213	.0053334
_cons	4.531922	.0301251	150.44	0.000	4.472819	4.591026

$$SBP = 4.531922 + 0.0044274 * \text{age}$$

This indicates that SBP will increase 0.004 per age (year).

Practice 4

Regression analysis (3)

- Please transform age variable into 10-year age group.

STATA : **gene age10=floor(age/10)**

- Let's see the association between age and systolic blood pressure using this variable (age10).
- What do you expect?



```
. reg lsbp age10
```

Source	SS	df	MS	Number of obs = 1210		
Model	2.8196114	1	2.8196114	F(1, 1208) = 90.90		
Residual	37.4689035	1208	.031017304	Prob > F = 0.0000		
Total	40.2885149	1209	.033323834	R-squared = 0.0700		
				Adj R-squared = 0.0692		
				Root MSE = .17612		
lsbp	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
age10	.0431853	.0045294	9.53	0.000	.0342989	.0520717
_cons	4.557933	.0276	165.14	0.000	4.503784	4.612083

$$\text{SBP} = 4.557933 + 0.0431853 * \text{age}(10)$$

$$\text{cf. SBP} = 4.531922 + 0.0044274 * \text{age}$$

Practice 4

Regression analysis (4)

- Suppose, **hemoglobin** level may be one of the predictors of **systolic blood pressure**.
- Please pick-up other potential predictors (other than hemoglobin) for systolic blood pressure in this data set based on your knowledge.
- And, conduct regression analysis.



How many explanatory variables can we use in a model?

Model	Number of explanatory variables	Example
Linear regression model	Sample size / 15	Up to around 6-7 variables in 100 subjects
Logistic regression model	Smaller sample size of outcome / 10	Up to 10 variables if the numbers of cases and controls are 100 and 300, respectively.
Cox proportional hazard model	The number of event / 10	Up to 9 variables if you have 90 events out of 150 subjects



ATTENTION!

- **When you include categorical variable in your model, you have to count that variable as (**the number of categories – 1**).**
 - **For example, the variable of age group used in the previous practice, we have to count it as “two” (=3 categories – 1) variables.**