

Learning Bio- basic terms

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Outline

- 1 Introduction
- 2 Descriptive Statistics
 - Category
 - Summary measures
- 3 Inferential Statistics
 - Estimation - Confidence Interval
 - A point estimate - An interval estimate
 - Interpretation a confidence interval
- 4 Hypothesis testing - p value
 - Hypothesis testing
 - Hypotheses
 - p-value
 - The hypothesis testing procedure
 - Power of Test

Aim

For clinicians, understanding concepts and basic terms in statistics:

- to apply in reading and using information of published medical evidence
- to reinforce basic knowledge biostatistics required for designing research

Statistics - Biostatistics

- **Statistics**
 - a science (concepts, rules, procedures) - and art of dealing with data
 - to study of uncertainty, to obtain reliable results
- **Biostatistics** - an application of statistics to:
 - medicine
 - biological sciences (education, psychology, agriculture...)
- **Modern society**
 - Reading
 - Writing
 - Statistical thinking: to make the strongest possible conclusions from limited amounts of data.

Objectives $\Rightarrow$ Statistics

Objectives:

(1) Organize & summarize data

(2) Reach inferences: sample $\rightarrow$ population

$\Rightarrow$ Statistics:

- Descriptive statistics $\rightarrow$ (1)
- Inferential statistics: drawing of inferences $\rightarrow$ (2)
 - Estimation (point estimate & interval estimate $\rightarrow$ confidence interval)
 - Hypothesis testing $\rightarrow$ reaching a decision (p value)
 - Parametric statistics
 - Non-parametric statistics $\ll$ Distribution-free statistics
 - Modeling, Predicting

Why basic terms?

- empowering belief:
 $\text{Statistics} = \text{Terms} + (\text{Normal distribution} + \text{Others})$
- and,
 $\text{Terms} = \text{Basic terms} + \text{Others}$

Descriptive Statistics

- to categorize available data by grouping
- to describe its distribution by calculating summary measures

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Grouping

- Raw data needs to be organized - to be presented in a clearer way.
- Data must be grouped into categories, as an example below:

Age (years-old)	Frequency	Relative frequency	Cumulative frequency
Under 20	100	20%	100
20 - 39	350	70%	450
40 or over	50	10%	500

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Calculating summary data

Three summary measures:

- Mean (average) = Sum of all data / n
- Median = 50th percentile value
- Mode = Most frequent value(s)

Measures of dispersions

Four measures to show how data is spread around the summary measures (variability)

- Range from minimum to maximum
- Variance = Mean of squared differences of values from a mean
- Standard deviation (SD) = Square root of the variance.
 - SD indicates the mean of differences of values from the mean.
 - It measures absolute dispersion.
- Coefficient of variance (CV) = Ratio of SD to the mean.
 - CV indicates the extent of variability in relation to the mean.
 - It measures relative dispersion.
 - There is no unit to measure CV, therefore they can be compared between any sets of data.

The measures of position

- Two measures of position:
 - Percentile = percent of values at or below
 - Quartile = 25th, 50th, and 75th percentiles
 - Z-score = a standardized value indicating a distance between the value and the mean divided by (in units of) the standard deviation.

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Why estimation?

- **Two reasons:**
 - Infinite populations: incapable of complete examination
 - Finite populations: cost, time
- In addition, estimation can help **not to defer a conclusion** until the whole population is observed

Estimators

- mean(s):
 - a single population mean: $\bar{x} \rightarrow \mu$
 - the difference between two population means - unpaired, paired: $(\bar{x}_1 - \bar{x}_2) \rightarrow (\bar{\mu}_1 - \bar{\mu}_2)$
- proportion(s):
 - a single population proportion: $\hat{p} \rightarrow p$ or $\hat{p} \rightarrow \pi$
 - the difference of two population proportions: $(\hat{p}_1 - \hat{p}_2) \rightarrow (\pi_1 - \pi_2)$
- variance(s):
 - a single population variance: $s^2 \rightarrow \sigma^2$
 - the ratio of two population variances: $\frac{s_1^2}{s_2^2} \rightarrow \frac{\sigma_1^2}{\sigma_2^2}$

An estimation of these parameters

An estimation of these parameters:

- Point estimate
- Interval estimate

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A point estimate

Estimator $\rightarrow$ Parameter

In many cases, a parameter may be estimated by more than one estimator.

- Example:
 - Sample mean $\rightarrow$ estimate population mean
 - Sample median $\rightarrow$ estimate population mean

An interval estimate

- In general, an interval estimate is obtained by the formula:
estimator $\pm$ (reliability coefficient) $\times$ (standard error)
- What is different is the source of the reliability coefficient:
In particular, when sampling is from a normal distribution with known variance, an interval estimate for μ may be expressed
as: $\bar{x} \pm z_{\alpha/2} \sigma_{\bar{x}}$

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How to interpret the interval

- In repeated sampling $100(1 - \alpha)\%$ of all intervals of the form will in the long run include the population mean, μ
- The quantity $(1 - \alpha)$, is called the **confidence coefficient** & The interval $\bar{x} \pm z_{\alpha/2} \sigma_{\bar{x}}$, is called the **confidence interval** for μ
- *The most frequently used values are: .90, .95, .99, which have associated reliability factors, respectively, of 1.645, 1.96, 2.58*

The practical interpretation

- We are $100(1 - \alpha)\%$ confident that the single computed interval $\bar{x} \pm z_{\alpha/2} \sigma_{\bar{x}}$ contains the population mean, μ
Example: ...
- E = margin error = maximum error = practical / clinical acceptable error:
$$E = z_{\alpha/2} \sigma_{\bar{x}} = z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

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Why hypothesis testing

- Hypothesis (H.): a statement concerns about some one or more populations
- Testing hypothesis: to aid researcher in **reaching a decision** concerning a population by examining a sample from that population

Hypothesis testing for

- mean(s)
 - a single population mean
 - the difference between two population means: unpaired, paired
- proportion(s)
 - a single population proportion
 - unpaired: a small sample, a sufficiently large sample
 - paired
 - the difference of two population proportions
- variance(s)
 - a single population variance
 - the difference of two population variances

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Two types of hypotheses

(1) Research Hypotheses:

- The conjecture or supposition
- It may be the results of years of observation
- Research H. leads directly to Statistical H.

(2) Statistical Hypotheses: Hypotheses are stated in such a way that they may be evaluated by appropriate statistical techniques.

- H_O
- H_A

Statistical Hypotheses

- H_O
 - The H_O is the hypothesis that is tested
 - The H_O should contain either $=, \leq, \geq$
(*The statement concerns about some one or more population's parameters in term of equality or inequality*)
- H_A
 - What we hope or expect to be able to conclude as a result of the test usually should be placed in the H_A
- The H_O & H_A are complementary
- One-sided vs. Two-sided Hypothesis Tests

Notes

- Neither hypothesis testing nor statistical inference, in general, leads to proof a hypothesis
- It merely indicates whether the hypothesis is supported or not supported by the available data
- When we fail to reject the H_0 , we do not say that it is true, but that it may be true
- When we speak of “accepting” a H_0 , we have this limitation in mind & do not wish to convey the idea that “accepting” implies proof

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p-value

Test statistic $\Rightarrow$ p-value

- General formula:

$$\text{Test statistic} = \frac{\text{relevant statistic} - \text{hypothesized parameter}}{\text{S.E. of the relevant statistic}} \Rightarrow \text{p-value}$$

$$\text{Example: } z = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$$

- p-value:
 - Probability of observing the difference **if** the H_0 is true.
 - An expression of how we believe in the H_0 .
 - Decision maker.
- p-value overdependence

Decision rule for a rejection or not the H_0

- α = type I error = level of significance (say, .01, .05, .10)
- β = type II error (say, .05, .10, .20)
- When we reject a $H_0 \iff p < \alpha$, risk of committing a type I error, rejecting a true H_0
- When we fail to reject a H_0 : risk of committing a type II error, “accepting” a false H_0

Type I & Type II error

Conditions under which type I & type II errors may be committed (the four possibilities)		Actual Situation (Truth in the population)	
		H_0 false	H_0 true
The results in the study sample → Conclusion:	Reject H_0	Correct decision	Type I error
	Fail to reject H_0	Type II error	Correct decision

Testing Hypothesis → Rejected or not rejected H_0

In the testing process, the H_0 either is rejected or is not rejected:

- If H_0 is not rejected, we will say that the data on which the test is based do not provide sufficient evidence to cause rejection
- If the testing process leads to rejection, we will say that the data at hand are not compatible with the H_0 , but are supportive of some other hypothesis & may be designated by H_A (H_A a contradiction statement of H_0)

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The Five-Step practical procedure for Hypothesis Testing (*opt.*)

- **Step 1:** Set up H_O , H_A
 - 1. Data: The nature of the data (classification)
 - 2. Assumptions: The normality of the population distribution, equality of variances, independence of samples. . .
 - 3. Hypotheses: H_O , H_A
- **Step 2:** Define the test statistic
 - 4. Test statistic
 - 5. Distribution of the Test Statistic

The Five-Step practical procedure for Hypothesis Testing, *cont. (opt.)*

- **Step 3:** Define a rejection region: having determined a value for α
 - 6. Decision rule
- **Step 4:**
 - 7. Calculate the value of the test statistic, and compare it with the acceptance & rejection regions that have already been specified.
 - 8. State our decision: to reject H_0 or to fail to reject H_0
- **Step 5:**
 - 9. Give a conclusion: this statement should be free of statistical jargon & should merely summarize the results of the analysis.

Note

A statistical package helps you only the step 4, but not for the other steps.

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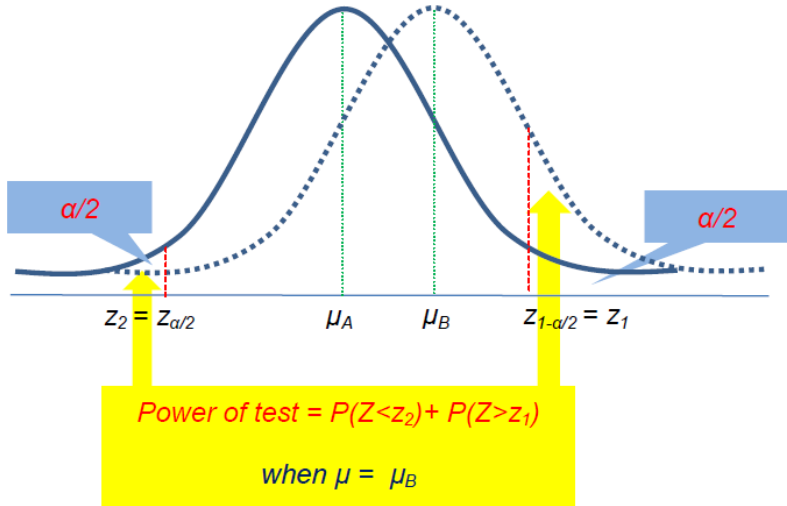
The Power of a Statistical Test (*opt.*)

- The probability of a type II error, β , has remained a phantom:
 - we know it is there,
 - but we don't know what it is
- One thing we can say is that: a wide C.I. for μ means that the corresponding 2-tailed test of H_0 versus H_A has a large chance of failing to reject a false H_0 ; that is β is large.

Determining β (*opt.*)

- $\beta = P(\text{fail to reject } H_0 \text{ when } H_0 \text{ is false})$
 $\iff 1 - \beta = P(\text{rejecting } H_0 \text{ when } H_0 \text{ is false})$
- $1 - \beta$ represents the probability of making a correct decision in the event that H_0 is false
- Since we like β to be small, that is we prefer $1 - \beta$ to be large
- The value of $1 - \beta$ is referred to as the power of test

Power of test (*opt.*)



Determination of sample size (*opt.*)

- Estimating a confidence interval: for descriptive purposes, investigators just need to consider the type I error.
- Testing a hypothesis: both type I & II errors need to be taken into account.
- When the sample size is fixed, because of some logistical reasons (financial, and/or time constrains):
 - the precision of the available data, and
 - whether this is meaningful for the study objective.

Summary

① Statistics:

- Descriptive statistics → organize & summarize data
- Inferential statistics → drawing of inferences
 - Estimation
 - Hypothesis testing
 - Modeling

② Estimation - confidence interval, estimator - very helpful as it gives a range of likely values

③ Hypothesis testing - p-value, or “surprise-level” value

Exercises

- ① A survey of 100 delivery cases in a population gave us the mean of newborn baby weight is 3,050 grams; 95% confidence interval is of (2,950 - 3,150 grams). Please give your explanation for the results.
- ② Please give your brief explanations of the p value.
 - ① ...
 - ② ...
 - ③ ...